

RAMAKRISHNA MISSION VIDYAMANDIRA

(Residential Autonomous College affiliated to University of Calcutta)

B.A./B.Sc. THIRD SEMESTER EXAMINATION, MARCH 2022

SECOND YEAR [BATCH 2020-23]

COMPUTER SCIENCE (HONOURS)

Date : 02/03/2022

Time : 11 am – 1 pm

Paper : V [CC5]

Full Marks : 50

Answer **any five** questions of the following:

[5×10]

1. a) Explain proof of correctness for finding the maximum element of an array.
b) Explain potential method of amortized analysis of an algorithm with example. [5+5]
2. a) Explain the basic structure of genetic algorithm.
b) Solve the following recurrence relation.
$$T(1) = \theta(1) \text{ and } T(n) = \sum_{i=1}^{n-1} T(i) + 1$$
 [5+5]
3. a) Write down various mutation operators of genetic algorithm.
b) Explain reduction. Why it is useful in computational complexity?
c) Explain backtracking with respect to 4-Queen's problem. [3+(2+2)+3]
4. a) Differentiate between backtracking and branch and bound algorithms.
b) Find out the time complexity of the following code segment.

```
int f(int n)
{
  if(n <= 2)
  {
    return 1;
  }
  else
  {
    return (f( $\sqrt{n}$ ) + 1);
  }
}
```


c) Explain why the concept of prefix code is necessary in Huffman coding. [3+4+3]
5. a) Find an optimal parenthesization of a matrix chain product whose sequence of dimensions is $\langle 4, 5, 3, 2, 7, 2 \rangle$.
b) What value does PARTITION procedure of QUICKSORT return when all elements in the array $A[p \dots r]$ have the same value? Explain. [6+4]
6. a) What is the optimal Huffman code for the following set of frequencies, based on first eight Fibonacci numbers?
a:1 b:1 c:2 d:3 e:5 f:8 g:13 h:21
b) How would you modify Strassen's algorithm to multiply $n \times n$ matrices in which n is not an exact power of 2? [5+5]

7. a) Consider an undirected graph with vertices labeled from 0 to 7 with the following edges. 0-1, 0-6, 0-7, 1-4, 1-6, 1-7, 2-3, 2-4, 2-5, 3-4, 3-6, 3-7, 5-6 Run BFS on the graph starting at node 0 and exploring edges incident to a vertex in numerical order of the labels of the vertex at the other end. Draw the BFS tree of the discovered edges produced by this algorithm.
- b) Solve the following 0-1 knapsack problem using dynamic programming. Number of items = 4, Maximum capacity of the knapsack = 5 units, Weight of each item = 2,3,4,5 units respectively, Profit of each item = 3,4,5,6 units respectively.

[5+5]

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